

Field-Induced Magnetic Ordering in the Quantum Spin System KCuCl_3

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KCuCl_3 is a three-dimensional coupled spin-dimer system and has a singlet ground state with an excitation gap $\Delta/k_B = 31$ K. High-field magnetization measurements for KCuCl_3 have been performed in static magnetic fields of up to 30 T and in pulsed magnetic fields of up to 60 T. The entire magnetization curve including the saturation region was obtained at $T = 1.3$ K. From the analysis of the magnetization curve, it was found that the exchange parameters determined from the dispersion relations of the magnetic excitations should be reduced, which suggests the importance of the renormalization effect in the magnetic excitations. The field-induced magnetic ordering accompanied by the cusplike minimum of the magnetization was observed as in the isostructural compound TlCuCl_3 . The phase boundary was almost independent of the field direction, and is represented by the power law. These results are consistent with the magnon Bose-Einstein condensation picture for field-induced magnetic ordering.

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I. INTRODUCTION

Recently, the physics of coupled antiferromagnetic spin-dimer systems has been attracting considerable attention from the viewpoints of magnetic excitations [1–10], the magnetization processes including magnetization plateaus [11–18] and field-induced three-dimensional (3D) magnetic ordering [19–25]. This study is concerned with the magnetization process of and the field-induced 3D magnetic ordering in KCuCl_3 , which is an $S = \frac{1}{2}$ coupled antiferromagnetic spin-dimer system and has a singlet ground state with an excitation gap (spin gap) $\Delta/k_B = 31$ K [2, 3, 26–28].

KCuCl_3 has a monoclinic structure (space group $P2_1/c$) [29]. The crystal structure is composed of planar dimers of Cu_2Cl_6 . The dimers are stacked on top of one another to form infinite double chains parallel to the crystallographic a -axis. These double chains are located at the corners and center of the unit cell in the $b-c$ plane as shown in Fig. 1. From the structural point of view, KCuCl_3 was first assumed to be a double chain spin system [26, 27]. The magnetic excitations in KCuCl_3 have been extensively investigated through neutron inelastic

scattering [2, 3, 30–34] and ESR measurements [28]. The effective dimer approximation [3, 34] and the cluster series expansion [7] were successfully applied to analyze the dispersion relations obtained. From these analyses, it was found that the origin of the spin gap is the strong antiferromagnetic interaction in the chemical dimer Cu_2Cl_6 , and that the neighboring dimers are weakly coupled not only along the double chain, but also in the $(1, 0, -2)$ plane, in which the hole orbitals of Cu^{2+} spread. Consequently, KCuCl_3 was characterized as a weakly and three-dimensionally coupled spin-dimer system.

KCuCl_3 differs from isostructural TlCuCl_3 and NH_4CuCl_3 in magnetic character. TlCuCl_3 also has a gapped ground state, however, the gap is considerably suppressed due to strong interdimer interactions [8, 23, 25, 27, 35]. On the other hand, NH_4CuCl_3 has a gapless ground state at zero magnetic field [36]. The remarkable feature of NH_4CuCl_3 is the existence of magnetization plateaus at one-quarter and three-quarters of the saturation magnetization [12, 37].

When a magnetic field is applied in the spin gap system, the gap Δ is suppressed and closes at $H_g = \Delta/g\mu_B$. For $H > H_g$ the system can undergo magnetic ordering due to 3D interactions with decreasing temperature. Such field-induced magnetic ordering was observed in the isostructural TlCuCl_3 [23–25]. For the field-induced magnetic ordering, two characteristic features which cannot be explained by the mean-field approach from the real space [38, 39] have been observed, irrespective of the applied field direction, when the applied field H is slightly higher than H_g . One is that the magnetization has a cusplike minimum at the transition temperature T_N . The other is that the phase boundary between the paramagnetic phase and the ordered phase can be expressed by the power law

$$[H_N(T) - H_g] \propto T^\phi, \quad (1)$$

with $\phi = 2.1(1)$. Here, $H_N(T)$ denotes the transition field at temperature T . These features can be understood in terms of the Bose-Einstein condensation (BEC) of excited triplets (magnons) [19–22].

When H is slightly higher than H_g , the density of magnon n which corresponds to the uniform magnetization is small. In this case, the system can be mapped onto the dilute magnon model. Using the Hartree-Fock

approximation, Nikuni *et al.* [20] demonstrated that the magnetization has the cusplike minimum at the transition temperature where the BEC of magnons occurs and that the phase boundary can be described by eq. (1) with $\phi = \frac{3}{2}$. Although the theoretical exponent is somewhat smaller than the experimental value $\phi = 2.1$, the magnon BEC theory gives a good description of the experimental results for TiCuCl_3 .

The magnetic anisotropy is negligible in KCuCl_3 [27] as it is in TiCuCl_3 [23, 24]. Therefore, the previously mentioned characteristic features for the magnon BEC should also be observed in KCuCl_3 , because the magnon BEC is universal in the isotropic spin gap system. With this motivation, we carried out magnetization measurements in static high magnetic fields above the gap field $H_g \approx 20$ T using a hybrid magnet. Since the entire magnetization curve in KCuCl_3 has not been observed, we also performed magnetization measurements in pulsed high magnetic fields of up to 60 T. As shown below, the saturation of the magnetization was observed at $H_s \sim 50$ T. From the saturation field H_s , it was found that the exchange parameters determined from the analyses of the dispersion should be reduced. This suggests the importance of the renormalization effect in the magnetic excitations in KCuCl_3 .

II. EXPERIMENTAL DETAILS

The single crystals of KCuCl_3 were prepared by the Bridgman method. The details of sample preparation were almost the same as those for TiCuCl_3 [23]. For KCuCl_3 , the temperature of the center of the furnace was set at 500°C. Single crystals of size $0.5\sim5$ cm³ were obtained. The crystals are easily cleaved along the $(1, 0, \bar{2})$ plane. The second cleavage plane is $(0, 1, 0)$. These cleavage planes are perpendicular to each other.

The high-field magnetization process in KCuCl_3 was measured at $T = 1.3$ K using an induction method with a multilayer pulse magnet at the Research Center for Materials Science at Extreme Conditions (KYOKUGEN), Osaka University. The magnetic fields were applied perpendicularly to the $(1, 0, \bar{2})$ plane and along the $[2, 0, 1]$ direction which is parallel to both cleavage $(1, 0, \bar{2})$ and $(0, 1, 0)$ planes. We used a single crystal in the measurement for $H \parallel [2, 0, 1]$. For $H \perp (1, 0, \bar{2})$ measurement, we stacked several single crystals along the cylindrical axis of the sample holder.

The temperature dependence of the magnetization of KCuCl_3 was measured in static magnetic fields of up to 30 T by a sample-extraction method with a 40 T-class hybrid magnet at the National Institute for Materials Science, Tsukuba. The magnetic fields were applied perpendicularly to the cleavage $(0, 1, 0)$ and $(1, 0, \bar{2})$ planes, and along the $[2, 0, 1]$ direction. These field directions were perpendicular to one another.

III. RESULTS AND DISCUSSIONS

A. Magnetization Process

Figure 2 shows the magnetization curves of KCuCl_3 measured at $T = 1.3$ K for $H \perp (1, 0, \bar{2})$ and $H \parallel [2, 0, 1]$. Here, the magnetization curves are normalized with the g -factors, *i.e.*, $g = 2.26$ for $H \perp (1, 0, \bar{2})$ and $g = 2.04$ for $H \parallel [2, 0, 1]$, which were obtained by ESR measurements. The magnetization curves for two different field directions almost coincide with each other when normalized by the g -factor, although the data for $H \parallel [2, 0, 1]$ are somewhat scattered. This implies that the difference between the transition fields H_g and the saturation fields H_s for $H \perp (1, 0, \bar{2})$ and $H \parallel [2, 0, 1]$ is attributed to the anisotropy of the g -factor, and that the magnetic anisotropy is negligible, as previously concluded [27]. Due to the spin gap, the magnetization is almost zero up to the transition field $(g/2)H_g = 23$ T, and increases rapidly and monotonically, and then saturates at $(g/2)H_s = 54$ T. As shown in Fig. 2, the slope of the magnetization in the vicinity of H_g and H_s is steeper than that in the intermediate field region. This behavior arises due to the quantum fluctuation.

In the magnetization slope region between H_g and H_s , transverse spin components have a long-range order. Since the lowest magnetic excitations occur at $\mathbf{Q} = (0, 0, 1)$ and its equivalent reciprocal lattice points, we assume that the spin ordering equivalent to that observed in TiCuCl_3 is realized in the ordered state (see Fig. 3). For the exchange interactions shown in Fig. 3, we use the notation given in ref. [7]: the main intradimer exchange is denoted as J . $J_{(lmn)}$ and $J'_{(lmn)}$ denote the exchange interactions between dimers separated by a lattice vector $l\mathbf{a} + m\mathbf{b} + n\mathbf{c}$. Applying the mean-field approximation to the interdimer interactions, we calculate the magnetization curve for the ground state. The details of the calculation are given in the Appendix.

In Table I, we list the exchange parameters in KCuCl_3 as determined by Müller and Mikeska [7]. They applied a cluster series expansion to analyze the dispersion relations observed in KCuCl_3 [3]. Their theory describes the experimental results, and the individual interdimer exchange parameters which cannot be obtained by the effective dimer approximation were determined. However, they used the same intradimer exchange interaction, $J = 4.25$ meV, as that obtained from the effective dimer approximation [3].

The dotted line in Fig. 4 is the magnetization curve calculated with the exchange parameters obtained by Müller and Mikeska [7]. We also plotted the experimental result obtained at $T = 1.3$ K for $H \perp (1, 0, \bar{2})$. The calculated gap field H_g coincides with the experimental value, while the calculated saturation field H_s is considerably larger than the experimental value. We infer that

the saturation field of eq. (A9) in the Appendix is close to the rigorous solution, because even for the $S = \frac{1}{2}$ 1D antiferromagnet, the classical calculation gives the same saturation field as the rigorous solution [40]. Therefore, we have to reduce the exchange parameters. However, it is difficult to adjust all of the exchange parameters, because we have only two equations for H_g and H_s . Thus, we make a uniform reduction for all of the interdimer exchange parameters. The thin solid line in Fig. 4 is the result calculated with the parameters listed in Table I. The intradimer interaction J and the interdimer interaction $J_{(lmn)}$ or $J'_{(lmn)}$ are reduced by factors 0.9 and 0.8, respectively. Both the calculated gap field H_g and saturation field H_s coincide with experimental values. Hence, we suggest that the renormalization effect in the magnetic excitations cannot be neglected, although the present system is 3D. The renormalization factor $\pi/2$ in the $S = \frac{1}{2}$ 1D antiferromagnet is well known [41]. The difference between the calculated and experimental results for $H_g < H < H_s$ is due to the quantum fluctuation, which is not taken into account in the present calculation.

B. Field-induced magnetic ordering

As mentioned in the Introduction, the present system can undergo magnetic ordering at a low temperature, when the magnetic field H is higher than the gap field H_g . Figure 5 shows the low-temperature magnetization measured at various external fields above H_g for $H \parallel b$, $H \perp (1, 0, \bar{2})$ and $H \parallel [2, 0, 1]$. With decreasing temperature, the magnetization exhibits a cusplike minimum, irrespective of the field direction, as observed in isostructural TiCuCl_3 . We assign the temperature with a cusplike minimum in the magnetization to the transition temperature T_N . However, there is a certain degree of error in determining the transition points, because the experimental data are somewhat scattered.

When the magnetic field is slightly higher than the gap field H_g , the number of created triplets (magnons) is small. Through the transverse components of the interdimer exchange interactions, the magnons can hop to the neighboring dimers in the same way as particles, which have bosonic natures. The longitudinal component of the interdimer exchange interaction gives rise to the interaction between magnons. Hence, the system can be mapped onto the interacting dilute boson system, and the phase transition can be described by the formation of the coherent state of dilute magnons, *i.e.*, Bose-Einstein condensation (BEC) [19–21]. The cusplike minimum of the temperature variation of the magnetization is characteristic of the BEC of the dilute magnons [20], and cannot be described by the mean-field approach from the real space [38, 39]. It is known that the mean-field approximation gives a reasonable description of the physical

quantities at $T = 0$, while it does not at finite temperatures. The mean-field approach gives the temperature-independent magnetization below T_N . The density of magnons n corresponds to the magnetization per Cu^{2+} ion m , *i.e.*, $m = (g/2)\mu_B n$. The reason that the magnetization increases again below T_N is because the increase of the number of condensed magnons is greater than the decrease of the number of thermally excited noncondensed magnons, so that the total number of magnons increases below T_N . The present experimental result is consistent with the magnon BEC theory of the phase transition.

The increase of the magnetization below T_N becomes smaller with increasing magnetic field. At $H = 30$ T, the density of magnons n is $n \approx 0.2$. For this large value of n , the condition of dilute magnons is no longer satisfied. In the dense magnon region, the hopping of magnon is significantly suppressed, and thus, the mean-field approach from the real space may give a better description of the phase transition.

The transition temperature T_N and transition field obtained for $H \parallel b$, $H \perp (1, 0, \bar{2})$ and $H \parallel [2, 0, 1]$ are plotted in Fig. 6. Since the phase boundary depends on the g -factor, we normalize the phase diagram by the g -factor. The g -factors used are $g = 2.05$ for $H \parallel b$, $g = 2.26$ for $H \perp (1, 0, \bar{2})$ and $g = 2.04$ for $H \parallel [2, 0, 1]$, which were determined by ESR measurements. Figure 7 shows the phase diagram normalized by the g -factor. The phase boundaries for three different field directions almost coincide when normalized by the g -factor, although the boundary for $H \perp (1, 0, \bar{2})$ tends to deviate from the others at around $(g/2)H \sim 30$ T. This result may reconfirm that the magnetic anisotropy is negligible in KCuCl_3 , as in TiCuCl_3 .

The phase boundary near the gap field can be described by the power law of eq. (1), as predicted by the magnon BEC theory [20]. We fit eq. (1) to the data for $T < 3$ K, for which $n < 0.03$. The solid line in Fig. 7 is the fitting with $\phi = 2.3(1)$ and $(g/2)H_g = 22.6(1)$ T. This exponent ϕ is close to $\phi = 2.1(1)$ observed in TiCuCl_3 [24, 25]. The exponent $\phi = 2.3$ obtained by the present measurements is somewhat larger than the value $\phi = \frac{3}{2}$ predicted by the magnon BEC theory [20]. We note that the exponent depends on the temperature region used for fitting. If we use the data up to higher temperatures, we have a larger exponent. This is because the ordered phase exists in a closed area in the magnetic field vs temperature diagram, and thus the entire phase boundary cannot be described by the power law with a single exponent. Since the low-temperature data contribute greatly to the determination of the exponent ϕ for the phase boundary near the gap field, the measurements at lower temperatures are needed.

The increase of the transition field obeying the power law with increasing temperature cannot be described in terms of the mean-field approach from the real space [38, 39] or the temperature dependence of the excitation

gap [33]. The mean-field result gives the transition field almost independent of temperature at low temperatures. The temperature dependence of the excitation gap was investigated by means of neutron scattering [33]. The gap is almost independent of temperature up to approximately 10 K, and then increases significantly.

IV. CONCLUSION

We have presented the results of magnetization measurements on the coupled spin-dimer system KCuCl_3 . The entire magnetization curve including the saturation region was obtained at $T = 1.3$ K, using pulsed magnetic fields up to 60 T. Applying mean-field approximation on the interdimer interactions, we analyzed the magnetization curve. It was found that the exchange parameters determined from the dispersion relations of the magnetic excitations should be reduced to fit both the gap field and the saturation field. This suggests the importance of the renormalization effect in the magnetic excitations.

The field-induced magnetic ordering was investigated in static magnetic fields up to 30 T. As observed in isostructural TiCuCl_3 , the magnetization exhibits a cusp-like minimum at the transition temperature. The phase boundary is almost independent of field direction, and is described by the power law. These features are compatible with the magnon BEC theory. Therefore, we conclude that the field-induced 3D magnetic ordering near the gap field in isotropic spin gap systems such as KCuCl_3 and TiCuCl_3 is universally represented by the BEC of dilute magnons.

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APPENDIX A: DERIVATION OF THE MAGNETIZATION CURVE

We calculate the magnetization curve at $T = 0$, assuming that the triplet excitations are created only on the dimer site. The interdimer interactions are treated by the mean-field approximation. In the magnetization slope region, the transverse spin components form the long-range order. Since the lowest magnetic excitations in KCuCl_3 and TiCuCl_3 occur at the same reciprocal lattice points, *i.e.*, $\mathbf{Q} = (h, 0, l)$ with integer h and odd l in the $a^* - c^*$ plane [2, 3, 8, 9], we can assume that the spin

structure in the ordered phase in KCuCl_3 is equivalent to that observed in TiCuCl_3 (see Fig. 3) [25]. We express the spin state of a dimer with the total spin $S = S_1 + S_2$ and the z component $S^z = S_1^z + S_2^z$ as $|S, S^z\rangle$, where subscript numbers 1 and 2 distinguish spins in a dimer. In the ordered phase, the transverse components of two spins on a dimer should be antiparallel and their magnitudes should be the same, *i.e.*, $\langle S^{x,y} \rangle = -\langle S_2^{x,y} \rangle$. This indicates that the spin state $|1, 0\rangle$ does not contribute to the basis state. Thus, we write the basis state of the j -th dimer as

$$\psi_j = |0, 0\rangle \cos \theta + (|1, 1\rangle \cos \varphi e^{i\phi_j} - |1, -1\rangle \sin \varphi e^{-i\phi_j}) \sin \theta. \quad (\text{A1})$$

Angles θ and φ were introduced to satisfy the normalization condition. The phase ϕ_j corresponds to the angle between the x -direction and the transverse component of the spin on the j -th dimer.

The average values of spin operators are given by

$$\begin{aligned} \langle S_{j,1}^z \rangle &= \langle S_{j,2}^z \rangle = \frac{1}{2} \sin^2 \theta \cos 2\varphi, \\ \langle S_{j,1}^+ \rangle &= -\langle S_{j,2}^+ \rangle = -\frac{1}{\sqrt{2}} \cos \theta \sin \theta (\cos \varphi + \sin \varphi) e^{-i\phi_j}, \\ \langle S_{j,1}^- \rangle &= -\langle S_{j,2}^- \rangle = -\frac{1}{\sqrt{2}} \cos \theta \sin \theta (\cos \varphi + \sin \varphi) e^{i\phi_j}. \end{aligned} \quad (\text{A2})$$

From the spin structure shown in Fig. 3, we see that all of the phases ϕ_j of dimers are the same in a chemical double chain, and that the phases of dimers in the double chains located at the corner and the center of the unit cell in the $b - c$ plane differ by π . With eq. (A2) and the exchange interactions shown in Fig. 3, the energy per dimer is expressed as

$$E = -\frac{3}{4} J \cos^2 \theta + \frac{1}{4} J \sin^2 \theta - g\mu_B H \sin^2 \theta \cos 2\varphi + \tilde{J} \sin^2 \theta \cos^2 \theta (1 + \sin 2\varphi) + \frac{1}{2} \bar{J} \sin^4 \theta \cos^2 2\varphi, \quad (\text{A3})$$

where

$$\tilde{J} = J_{(100)}^{\text{eff}} - 2J_{(1,\frac{1}{2},\frac{1}{2})}^{\text{eff}} + J_{(2,0,1)}^{\text{eff}}, \quad (\text{A4})$$

with

$$\begin{aligned} J_{(100)}^{\text{eff}} &= \frac{1}{2} (2J_{(100)} - J'_{(100)}) , \\ J_{(1,\frac{1}{2},\frac{1}{2})}^{\text{eff}} &= \frac{1}{2} (J_{(1,\frac{1}{2},\frac{1}{2})} - J'_{(1,\frac{1}{2},\frac{1}{2})}) , \\ J_{(2,0,1)}^{\text{eff}} &= -\frac{1}{2} J'_{(2,0,1)} \end{aligned} \quad (\text{A5})$$

and

$$\bar{J} = J_{(100)} + \frac{1}{2} J'_{(100)} + J_{(1,\frac{1}{2},\frac{1}{2})} + J'_{(1,\frac{1}{2},\frac{1}{2})} + \frac{1}{2} J'_{(2,0,1)}. \quad (\text{A6})$$

Angles θ and φ can be determined by $\partial E/\partial\theta = 0$ and $\partial E/\partial\varphi = 0$, which lead to

$$J - g\mu_B H \cos 2\varphi + \tilde{J} \cos 2\theta (1 + \sin 2\varphi) + \bar{J} \sin^2 \theta \cos^2 2\varphi = 0, \quad (\text{A7})$$

and

$$g\mu_B H \sin 2\varphi + \tilde{J} \cos^2 \theta \cos 2\varphi - \bar{J} \sin^2 \theta \cos 2\varphi \sin 2\varphi = 0, \quad (\text{A8})$$

for the ordered state between the gap field H_g and the saturation field H_s . The magnetization curve is obtained by solving eqs. (A7) and (A8) self-consistently.

At the saturation field H_s , $\sin \theta = 1$ and $\sin \varphi = 0$. Thus, H_s is given by

$$g\mu_B H_s = J - \tilde{J} + \bar{J}. \quad (\text{A9})$$

At the gap field H_g , $\sin \theta = 0$. Substituting this condition into eqs. (A7) and (A8), we obtain

$$g\mu_B H_g = \sqrt{J^2 + 2J\tilde{J}}. \quad (\text{A10})$$

It is noted that the right-hand side of eq. (A10) is equivalent to the lowest excitation energy given by the effective dimer approximation, in which the individual interdimer interactions $J_{(lmn)}$ and $J'_{(lmn)}$ are reduced to an effective interdimer interaction $J_{(lmn)}^{\text{eff}}$ as shown in eq. (A5) [3]. If we neglect the highest $|1, -1\rangle$ state, *i.e.*, $\sin \varphi \equiv 0$, we obtain

$$g\mu_B H_g = J + \tilde{J}. \quad (\text{A11})$$

This result can also be derived from the Tachiki-Yamada theory [38, 39].

[9] A. Oosawa, T. Kato, H. Tanaka, K. Kakurai, M. Müller and H. -J. Mikeska, Phys. Rev. B **65**, 094426 (2002).

[10] M. B. Stone, Y. Chen, J. Rittner, H. Yardimci, D. H. Reich, C. Broholm, D. V. Ferraris and T. Lectka, Phys. Rev. B **65**, 064423 (2002).

[11] Y. Narumi, M. Hagiwara, R. Sato, K. Kindo, H. Nakano and M. Takahashi, Physica B **246-247**, 509 (1998).

[12] W. Shiramura, K. Takatsu, B. Kurniawan, H. Tanaka, H. Uekusa, Y. Ohashi, K. Takizawa, H. Mitamura and T. Goto, J. Phys. Soc. Jpn. **67**, 1548 (1998).

[13] K. Totsuka, Phys. Rev. B **57**, 3454 (1998).

[14] A. K. Kolezhuk, Phys. Rev. B **59**, 4181 (1999).

[15] H. Kageyama, K. Yoshimura, R. Stern, N. V. Mushnikov, K. Onizuka, M. Kato, K. Kosuge, C. P. Slichter, T. Goto and Y. Ueda, Phys. Rev. Lett **82**, 3168 (1999).

[16] S. Miyahara and K. Ueda, Phys. Rev. Lett **82**, 3701 (1999).

[17] K. Onizuka, H. Kageyama, Y. Narumi, K. Kindo, Y. Ueda and T. Goto, J. Phys. Soc. Jpn. **69**, 1016 (2000).

[18] M. Uchida, H. Tanaka, M. I. Bartashevich and T. Goto, J. Phys. Soc. Jpn. **70**, 1790 (2001).

[19] T. Giamarchi and A. M. Tsvelik, Phys. Rev. B **59**, 11398 (1999).

[20] T. Nikuni, M. Oshikawa, A. Oosawa and H. Tanaka, Phys. Rev. Lett. **84**, 5868 (2000).

[21] S. Wessel and S. Haas, Phys. Rev. B **62**, 316 (2000).

[22] S. Wessel, M. Olshanii and S. Haas, Phys. Rev. Lett. **87**, 206407 (2001).

[23] A. Oosawa, M. Ishii and H. Tanaka, J. Phys.: Condens. Matter **11**, 265 (1999).

[24] A. Oosawa, H. Aruga Katori and H. Tanaka, Phys. Rev. B **63**, 134416 (2001).

[25] H. Tanaka, A. Oosawa, T. Kato, H. Uekusa, Y. Ohashi, K. Kakurai and A. Hoser, J. Phys. Soc. Jpn. **70**, 939 (2001).

[26] H. Tanaka, K. Takatsu, W. Shiramura and T. Ono, J. Phys. Soc. Jpn. **65**, 1945 (1996).

[27] W. Shiramura, K. Takatsu, H. Tanaka, K. Kamishima, M. Takahashi, H. Mitamura and T. Goto, J. Phys. Soc. Jpn. **66**, 1900 (1997).

[28] H. Tanaka, T. Takatsu, W. Shiramura, T. Kambe, H. Nojiri, T. Yamada, S. Okubo, H. Ohta and M. Motokawa, Physica B **246-247**, 545 (1998).

[29] R. D. Willett, C. Dwiggins, R. F. Kruh and R. E. Rundle, J. Chem. Phys. **38**, 2429 (1963).

[30] T. Kato, A. Oosawa, K. Takatsu, H. Tanaka, W. Shiramura, K. Nakajima and K. Kakurai, J. Phys. Chem. Solids **60**, 1125 (1999).

[31] N. Cavaldini, W. Henggler, A. Furrer, H.-U. Güdel, K. Krämer and H. Mutka, Physica B **276-278**, 540 (2000).

[32] N. Cavaldini, G. Heigold, W. Henggeler, A. Furrer, H.-U. Güdel, K. Krämer and H. Mutka, J. Phys.: Condens. Matter **12**, 5463 (2000).

[33] N. Cavaldini, Ch. Rüegg, W. Henggeler, A. Furrer, H.-U. Güdel, K. Krämer and H. Mutka, Eur. Phys. J. B **18**, 565 (2000).

[34] T. Kato, A. Oosawa, H. Tanaka, K. Nakajima and K. Kakurai, J. Phys. Soc. Jpn. Suppl. A **70**, 160 (2001).

[35] K. Takatsu, W. Shiramura and H. Tanaka, J. Phys. Soc. Jpn. **66**, 1611 (1997).

[36] B. Kurniawan, M. Ishikawa, T. Kato, H. Tanaka, K. Tak-

-
- [1] A. W. Garrett, S. E. Nagler, D. A. Tennant, B. C. Sales and T. Barnes, Phys. Rev. Lett **79**, 745 (1997).
[2] T. Kato, K. Takatsu, H. Tanaka, W. Shiramura, M. Mori, K. Nakajima and K. Kakurai, J. Phys. Soc. Jpn. **67**, 752 (1998).
[3] N. Cavaldini, W. Henggler, A. Furrer, H.-U. Güdel, K. Krämer and H. Mutka, Eur. Phys. J. B **7**, 519 (1999).
[4] H. Kageyama, M. Nishi, N. Aso, K. Onizuka, T. Yoshihama, K. Nukui, K. Kodama, K. Kakurai and Y. Ueda, Phys. Rev. Lett **84**, 5876 (2000).
[5] K. Totsuka, S. Miyahara and K. Ueda, Phys. Rev. Lett **86**, 520 (2001).
[6] G. Xu, C. Broholm, D. H. Reich and M. A. Adams, Phys. Rev. Lett **84**, 4465 (2000).
[7] M. Müller and H. -J. Mikeska, J. Phys.: Condens. Matter **12**, 7633 (2000).
[8] N. Cavaldini, G. Heigold, W. Henggeler, A. Furrer, H.-U. Güdel, K. Krämer and H. Mutka, Phys. Rev. B **63**, 172414 (2001).

- izawa and T. Goto, J. Phys.: Condens. Matter **11**, 9073 (1999).
- [37] B. Kurniawan, H. Tanaka, K. Takatsu, W. Shiramura, T. Fukuda, H. Nojiri and M. Motokawa, Phys. Rev. Lett. **82**, 1281 (1999).
- [38] M. Tachiki and T. Yamada, J. Phys. Soc. Jpn. **28**, 1413 (1970).
- [39] M. Tachiki and T. Yamada, Suppl. Prog. Theor. Phys. No. 46, 291 (1970).
- [40] R. B. Griffiths, Phys. Rev. **133**, A768 (1964).
- [41] J. des Cloizeaux and J. J. Pearson, Phys. Rev. **128**, 2131 (1962).

TABLE I. Exchange interactions in KCuCl₃ in the unit of meV.

J	$J_{(100)}$	$J'_{(100)}$	$J_{(1, \frac{1}{2}, \frac{1}{2})}$	$J'_{(1, \frac{1}{2}, \frac{1}{2})}$	$J'_{(2, 0, 1)}$	ref.
4.25	-0.021	0.425	0.850	0.170	0.799	[7]
3.83	-0.017	0.340	0.680	0.136	0.639	this work

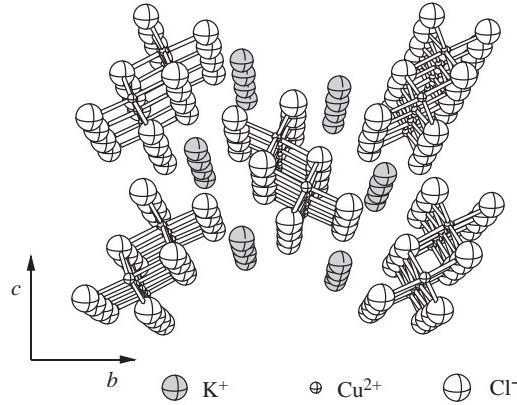


FIG. 1. Crystal structure of KCuCl_3 viewed along the a -axis. Shaded, small open and large open circles denote K^+ , Cu^{2+} and Cl^- ions, respectively.

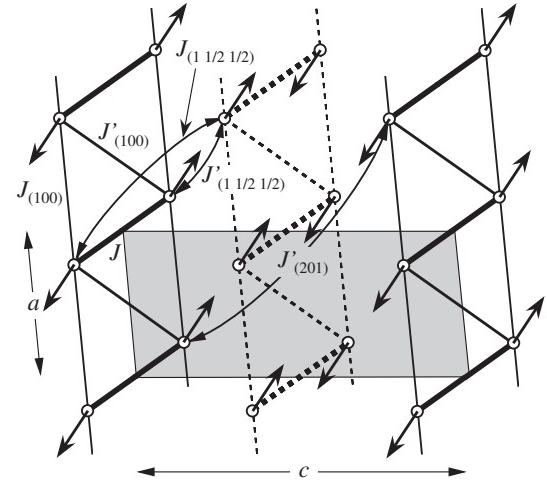


FIG. 3. Important exchange interactions in KCuCl_3 and the spin structure observed in the ordered phase of TlCuCl_3 for $H \parallel b$. The double chain located at the corner and the center of the chemical unit cell in the $b - c$ plane are represented by solid and dashed lines, respectively. The shaded area is the chemical unit cell in the $a - c$ plane.

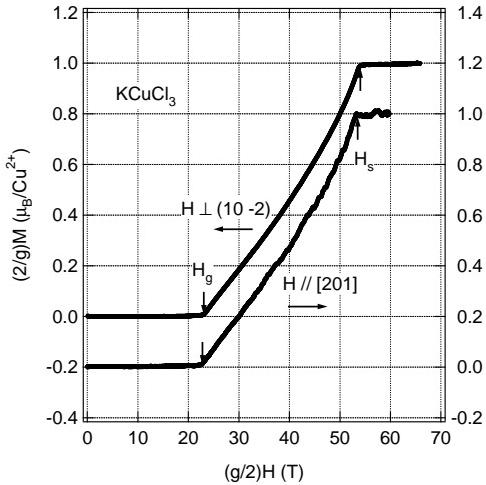


FIG. 2. Magnetization curve of KCuCl_3 measured at $T = 1.3$ K for the magnetic fields $H \parallel [2, 0, 1]$ and $H \perp (1, 0, \bar{2})$. The values of the magnetization and the magnetic field are normalized by the g -factor.

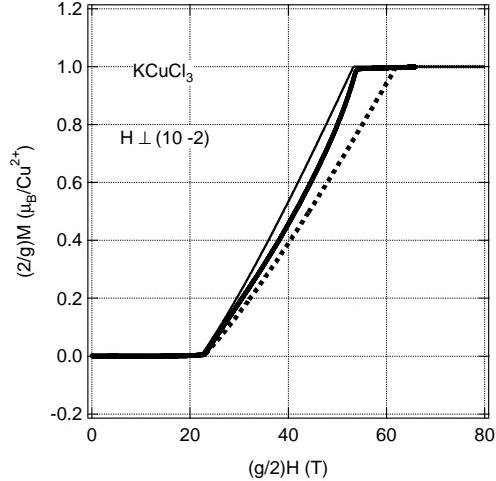
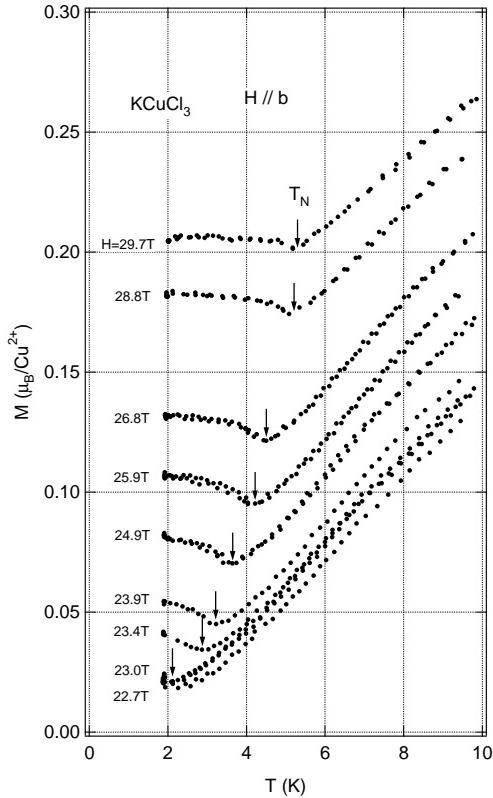
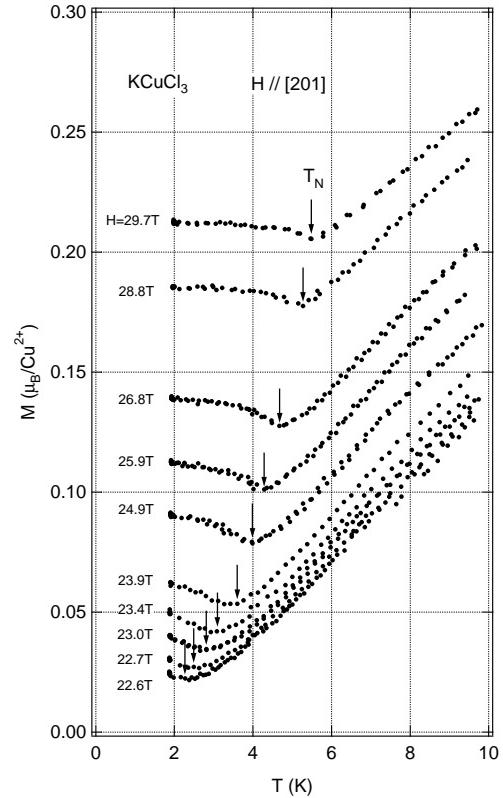


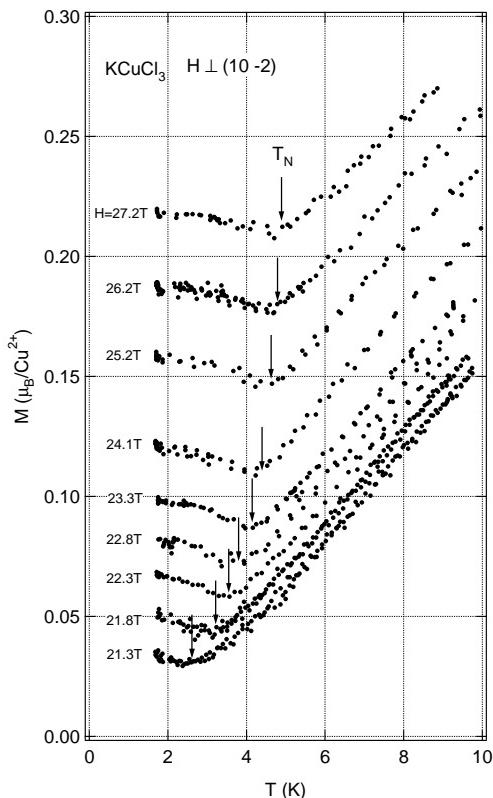
FIG. 4. Magnetization curve calculated by the mean-field approximation. The dotted and thin solid lines are the results with the exchange parameters obtained by Müller and Mikeska [7], and reduced ones, respectively. The thick solid line is the magnetization curve observed in KCuCl_3 for $H \perp (1, 0, \bar{2})$.



(a)



(c)



(b)

FIG. 5. Low-temperature magnetizations of KCuCl_3 measured at various external fields for (a) $H \parallel b$, (b) $H \perp (1, 0, \bar{2})$ and (c) $H \parallel [2, 0, 1]$.

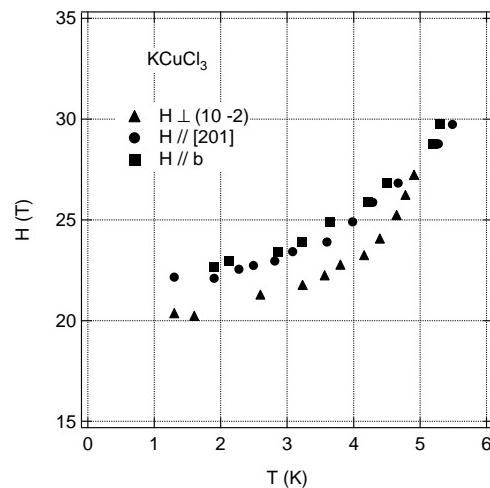


FIG. 6. Phase boundaries in KCuCl_3 obtained for three different field directions.

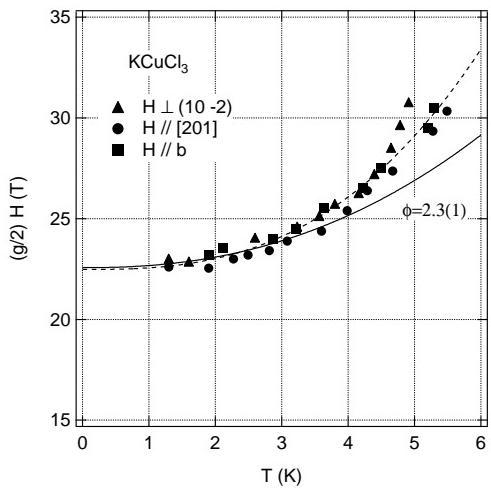


FIG. 7. Phase diagram in KCuCl_3 normalized by the g -factor. The solid line denotes the fitting by eq. (1) with $(g/2)H_g = 22.6(1)$ T and $\phi = 2.3(1)$. The dashed line is a visual guide.